



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

**SENIOR CERTIFICATE EXAMINATIONS/
SENIORSERTIFIKAAT-EKSAMEN
NATIONAL SENIOR CERTIFICATE EXAMINATIONS/
NASIONALE SENIORSERTIFIKAAT-EKSAMEN**

**MATHEMATICS P2/
WISKUNDE V2**

MARKING GUIDELINES/NASIENRIGLYNE

2021

**MARKS: 150
PUNTE: 150**

**These marking guidelines consist of 23 pages.
Hierdie nasienriglyne bestaan uit 23 bladsye.**

NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

LET WEL:

- *As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.*
- *As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, sien die doodgetrekte poging na.*
- *Volgehoue akkuraatheid word in ALLE aspekte van die memorandum toegepas. Hou op nasien by die tweede berekeningsfout.*
- *Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.*

GEOMETRY	
S	A mark for a correct statement (A statement mark is independent of a reason)
	<i>'n Punt vir 'n korrekte bewering ('n Punt vir 'n bewering is onafhanklik van die rede)</i>
R	A mark for the correct reason (A reason mark may only be awarded if the statement is correct)
	<i>'n Punt vir 'n korrekte rede ('n Punt word slegs vir die rede toegeken as die bewering korrek is)</i>
S/R	Award a mark if statement AND reason are both correct
	<i>Ken 'n punt toe as die bewering EN rede beide korrek is</i>

QUESTION/VRAAG 1

1.1

26	13	3	18	12	34	24	58	16	10	15	69	20	17	40
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1.1.1(a)	$\bar{x} = \frac{375}{15}$ $\bar{x} = 25 \text{ MB}$	Answer only: Full marks	✓ 375 ✓ answer	(2)
1.1.1(b)	$\sigma = 17,65 \text{ MB}$		✓ answer	(1)
1.1.2	$25 + 17,65 = 42,65$ $\therefore 2 \text{ days}$		✓ 42,65 ✓ 2	(2)
1.1.3	Overall $\bar{x} = \frac{80}{100} \times 25$ $= 20 \text{ MB}$ $\frac{375 + x}{30} = 20$ $x = 600 - 375$ $= 225$ maximum total amount of data that Sam must use for the remainder of the month: 225 MB		✓ Overall $\bar{x} = 20$ ✓ $\frac{375 + x}{30} = 20$ ✓ answer	(3)

1.2

Wind speed in km/h (x)	2	6	15	20	25	17	11	24	13	22
Temperature in °C (y)	28	26	22	22	16	20	24	19	26	19

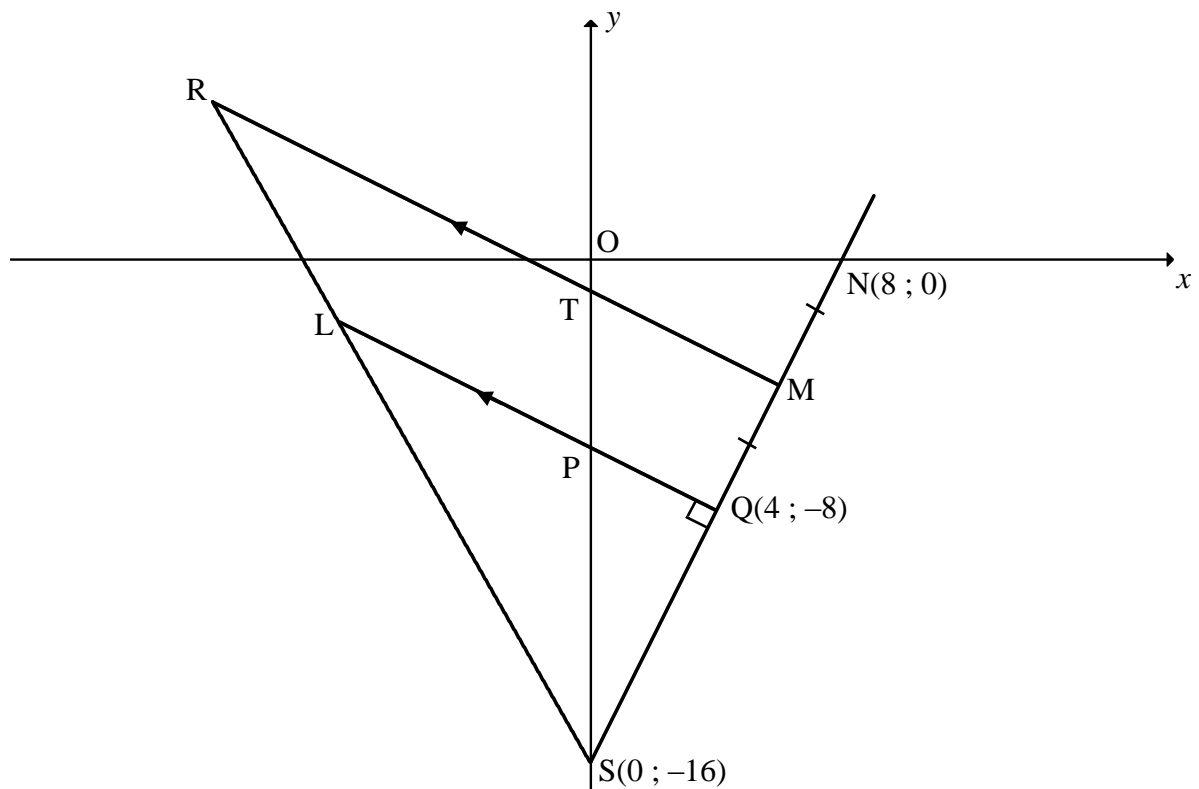
1.2.1	$a = 29,35$ $b = -0,46$ $\hat{y} = 29,35 - 0,46x$	✓ a ✓ b ✓ equation	(3)
1.2.2	$y = 25,20 \text{ °C}$ (calculator) OR $\hat{y} = 29,35 - 0,46(9)$ $y = 25,21 \text{ °C}$	✓✓ answer ✓ substitution ✓ answer	(2)
1.2.3	$b < 0$, indicating that as the wind speed increases the temperature decreases.	✓ interpretation	(1)
[14]			

QUESTION/VRAAG 2

Number of days absent	Number of learners	Cumulative frequency
$0 \leq x < 5$	34	34
$5 \leq x < 10$	45	79
$10 \leq x < 15$	98	177
$15 \leq x < 20$	43	220
$20 \leq x < 25$	7	227
$25 \leq x < 30$	3	230

2.1	Modal class: $10 \leq x < 15$	✓ answer (1)
2.2	177 learners	✓ answer (1)
2.3	230 learners	✓ answer (1)
2.4	<div style="text-align: center;"> <p>Ogive</p> </div>	✓ grounding at (0; 0) ✓ shape ✓ upper limits ✓ All other points correct (4)
2.5	The median is at position 115. <input type="checkbox"/> value of median is 12 days (accept 11 – 14) <div style="border: 1px solid black; padding: 2px; display: inline-block; margin-left: 10px;"> Answer only: Full marks </div>	✓ reading off at 115 ✓ answer (2)
[9]		

QUESTION/VRAAG 3

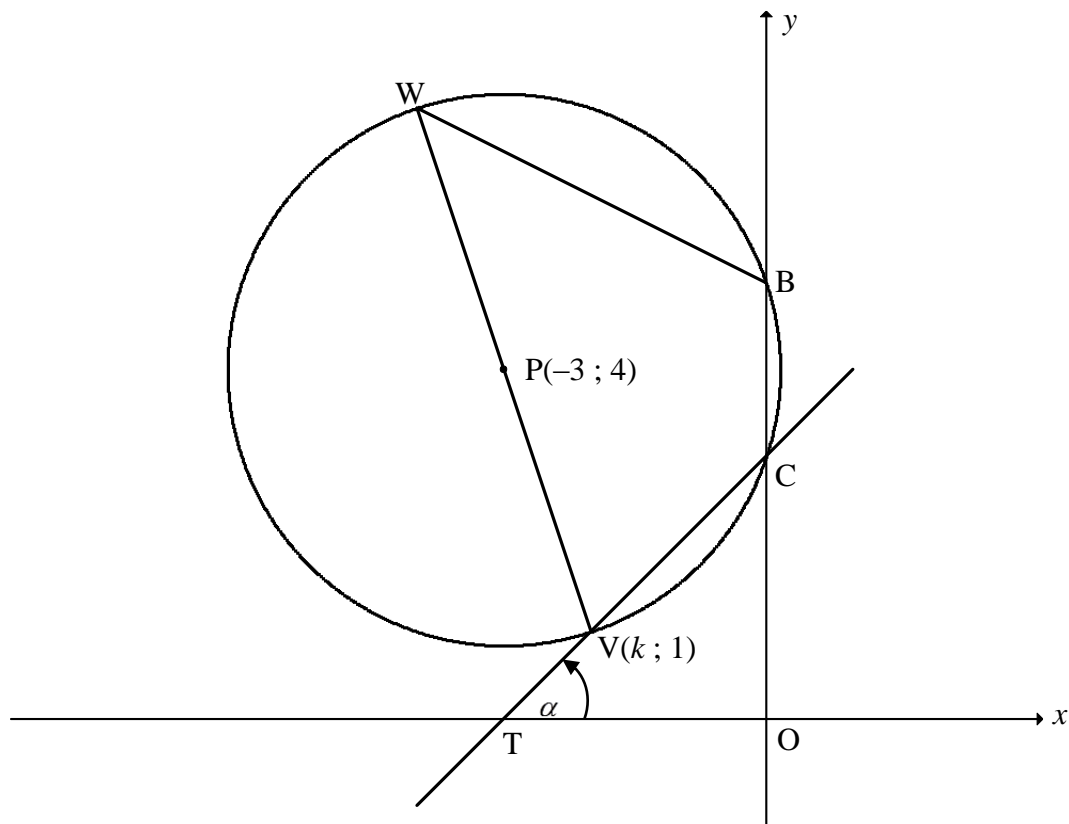


3.1	$M\left(\frac{4+8}{2}; \frac{-8+0}{2}\right)$ $M(6; -4)$		✓ x_M ✓ y_M (2)
3.2	$m_{NS} = \frac{0 - (-16)}{8 - 0} \text{ or } m_{NQ} = \frac{0 - (-8)}{8 - 4} \text{ or } m_{QS} = \frac{-8 - (-16)}{4 - 0}$ $= 2$		✓ subst N and Q or N and Q or Q and S into gradient formula ✓ answer (2)
3.3	$m_{LQ} \times 2 = -1 \quad [LQ \perp NS]$ $\therefore m_{LQ} = -\frac{1}{2}$ $-8 = -\frac{1}{2}(4) + c \quad \text{OR} \quad y + 8 = -\frac{1}{2}(x - 4)$ $c = -6 \quad \quad \quad y + 8 = -\frac{1}{2}x + 2$ $\therefore y = -\frac{1}{2}x - 6$		✓ m_{LQ} ✓ substitution of Q ✓ calculation of c or simplification (3)
3.4	OS is the radius of circle passing through S $(x - 0)^2 + (y - 0)^2 = (16)^2$ $x^2 + y^2 = 256$ <div style="border: 1px solid black; padding: 2px; display: inline-block; margin-left: 100px;">Answer only: Full marks</div>		✓ identifying radius = 16 ✓ Equation of circle (2)

<p>3.5</p>	$m_{RM} = m_{LQ} = -\frac{1}{2} \quad [RM \parallel LQ]$ $-4 = -\frac{1}{2}(6) + c \quad \text{OR} \quad y + 4 = -\frac{1}{2}(x - 6)$ $c = -1 \quad y + 4 = -\frac{1}{2}x + 3$ $\therefore y = -\frac{1}{2}x - 1$ <p>T(0; -1)</p>	<p>✓ m_{RM}</p> <p>✓ substitution of M(6; -4)</p> <p>✓ coordinates of T</p> <p>(3)</p>
<p>3.6</p>	<p>T(0; -1), P(0; -6) and S(0; -16)</p> <p>∴ PS = 10 units and TS = 15 units</p> $\frac{LS}{RS} = \frac{PS}{TS} = \frac{2}{3} \quad [prop\ theorem; RM \parallel LP]$ <p>OR [line ∥ one side of Δ/lyn ∥ een sy v Δ]</p> <div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 10px auto;"> <p>Answer only: Full marks</p> </div> <p>OR</p> <p>M(6 ; -4), Q(4 ; -8) and S(0 ; -16)</p> <p>MS = $\sqrt{180} = 6\sqrt{5}$ and QS = $\sqrt{80} = 4\sqrt{5}$</p> $\frac{LS}{RS} = \frac{QS}{MS} = \frac{2}{3} \quad [prop\ theorem; RM \parallel LQ]$ <p>OR [line ∥ one side of Δ/lyn ∥ een sy v Δ]</p> <div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 10px auto;"> <p>Answer only: Full marks</p> </div>	<p>✓ PS = 10 units</p> <p>✓ TS = 15 units</p> <p>✓ answer</p> <p>(3)</p> <p>✓ MS = $6\sqrt{5}$ units</p> <p>✓ QS = $4\sqrt{5}$ units</p> <p>✓ answer</p> <p>(3)</p>
<p>3.7</p>	<p>area of PTMQ = area of ΔTSM – area of ΔPSQ</p> $= \frac{1}{2} \cdot ST \cdot \perp h_M - \frac{1}{2} \cdot PS \cdot \perp h_Q$ $= \frac{1}{2}(15)(6) - \frac{1}{2}(10)(4)$ $= 45 - 20$ $= 25 \text{ square units}$ <p>OR</p> <p>TM = $\sqrt{45} = 3\sqrt{5} = 6,71$</p> <p>MQ = $\sqrt{20} = 2\sqrt{5} = 4,47$</p> <p>PQ = $\sqrt{20} = 2\sqrt{5} = 4,47$</p> <p>area of trapezium PTMQ = $\frac{1}{2}(3\sqrt{5} + 2\sqrt{5})(2\sqrt{5})$</p> $= \frac{1}{2}(5\sqrt{5})(2\sqrt{5})$ $= 25 \text{ square units}$	<p>✓ area of ΔTSM – area of ΔPSQ</p> <p>✓ area ΔTSM = 45</p> <p>✓ area ΔPSQ = 20</p> <p>✓ answer</p> <p>(4)</p> <p>✓ TM = $3\sqrt{5}$</p> <p>MQ = $2\sqrt{5}$</p> <p>PQ = $2\sqrt{5}$</p> <p>✓ area of trapezium = $\frac{1}{2}$ (sum of ∥sides)(height)</p> <p>✓ substitute into formula</p> <p>✓ answer</p> <p>(4)</p>

	<p>OR</p> $MQ = \sqrt{20} = 2\sqrt{5}$ $PQ = \sqrt{20} = 2\sqrt{5}$ $TP = 5$ <p>area of PTMQ = area of ΔMTP + area of ΔPQM</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $\text{area of PTMQ} = \frac{1}{2} TP \times \perp h_M + \frac{1}{2} MQ \times PQ$ </div> <p>area of PTMQ = $10 + 15 = 25$</p>	<p>✓ area of ΔMTP + area of ΔPQM</p> $\text{area of PTMQ} = \frac{1}{2}(5) \times 6 + \frac{1}{2}(2\sqrt{5})(2\sqrt{5})$ <p>✓ area $\Delta MTP = 10$ ✓ area $\Delta PQM = 15$ ✓ answer</p> <p style="text-align: right;">(4)</p>
	[19]	

QUESTION 4



<p>4.1</p>	<p> $PV = r = \sqrt{10}$ $PV = \sqrt{(k - (-3))^2 + (1 - 4)^2} = \sqrt{10}$ $(PV)^2 = (k - (-3))^2 + (1 - 4)^2 = 10$ $k^2 + 6k + 9 + 9 = 10$ OR $(k + 3)^2 + 9 = 10$ $k^2 + 6k + 8 = 0$ $(k + 3)^2 = 1$ $(k + 4)(k + 2) = 0$ $k + 3 = 1$ or $k + 3 = -1$ $k = -4$ or $k = -2$ $\therefore k = -2$ </p>	<p> ✓ $PV = r = \sqrt{10}$ ✓ substitution into distance formula ✓ standard form ✓ factors ✓ answer (5) </p>
<p>4.2</p>	<p> $x^2 + 6x + y^2 - 8y + 15 = 0$ y-intercepts: $(0)^2 + 6(0) + y^2 - 8y + 15 = 0$ $(y - 3)(y - 5) = 0$ $y_C = 3$ or $y_B = 5$ $\therefore BC = 2$ units </p>	<p> ✓ $x = 0$ ✓ factors ✓ both values ✓ answer (4) </p>

<p>4.3.1</p>	$m_{TC} = \frac{3-1}{0-(-2)}$ $= 1$ $\tan \alpha = 1$ $\therefore \alpha = 45^\circ$ <p>OR</p> $y = mx + 3$ $1 = m(-2) + 3$ $m_{TC} = 1$ $\tan \alpha = 1$ $\therefore \alpha = 45^\circ$	<p>✓ substitution into gradient formula</p> <p>✓ $\tan \alpha = 1$</p> <p>✓ answer (3)</p> <p>✓ substitution into equation of a line</p> <p>✓ $\tan \alpha = 1$</p> <p>✓ answer (3)</p>
<p>4.3.2</p>	$\hat{BCV} = 135^\circ$ <p>[ext \angle of Δ/buite \angle v Δ]</p> $\therefore \hat{VWB} = 45^\circ$ <p>[opp \angles of cyclic quad/teenoorst. \anglee v kvh]</p> <div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 0 auto;"> <p>Answer only: Full marks</p> </div> <p>OR</p> $\hat{TCO} = 45^\circ$ <p>[\angles of Δ/\anglee v Δ]</p> $\therefore \hat{VWB} = 45^\circ$ <p>[ext \angles of cyclic quad/buite \angle v kvh]</p> <div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 0 auto;"> <p>Answer only: Full marks</p> </div>	<p>✓ $\hat{BCV} = 135^\circ$</p> <p>✓ answer (2)</p> <p>✓ $\hat{TCO} = 45^\circ$</p> <p>✓ answer (2)</p>
<p>4.4.1</p>	<p>Q(-3; -2)</p>	<p>✓ x_Q ✓ y_Q (2)</p>
<p>4.4.2</p>	$(x+3)^2 + (y+2)^2 = 10$	<p>✓ LHS ✓ RHS (2)</p>
<p>4.4.3</p>	<p>$x = -2$ or $x = -4$</p>	<p>✓ $x = -2$ ✓ $x = -4$ (2)</p>
		<p>[20]</p>

QUESTION/VRAAG 5

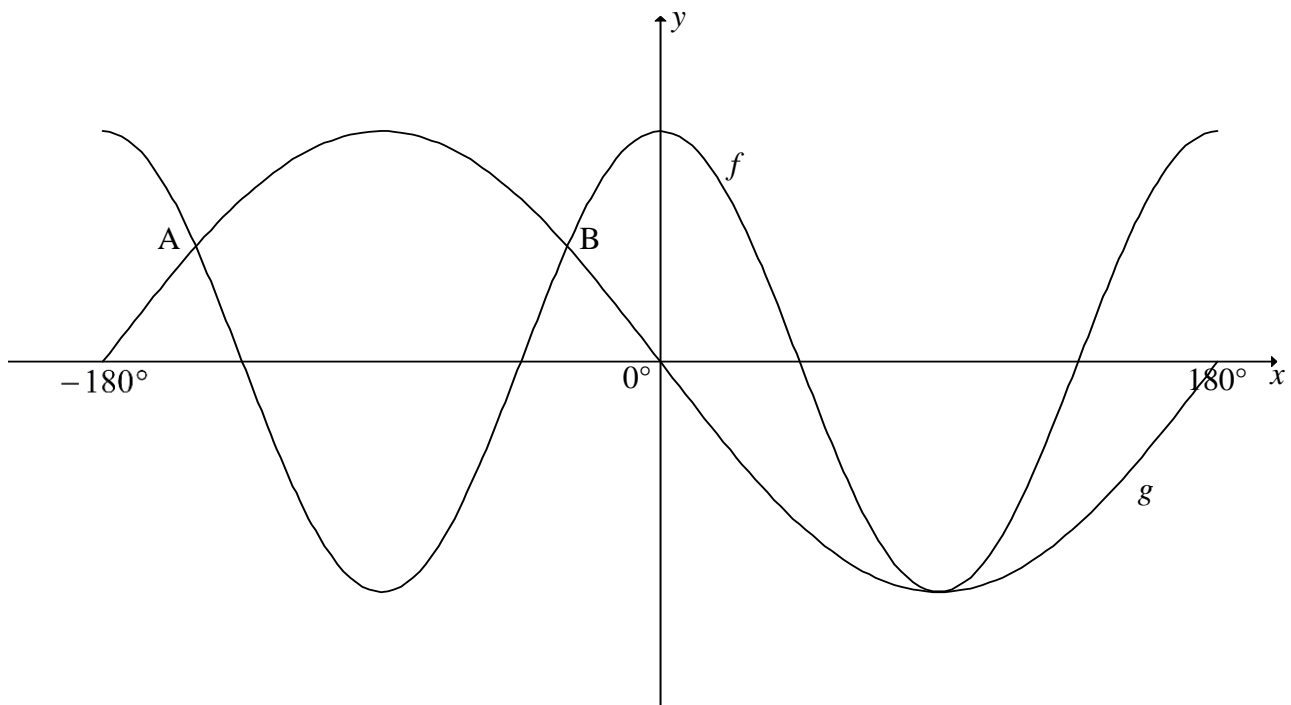
5.1	$\tan(-x) \cdot \cos x \cdot \sin(x - 180^\circ) - 1$ $= -\tan x \cdot \cos x \cdot \sin(-(180^\circ - x)) - 1$ $= \frac{-\sin x}{\cos x} \cdot \cos x \cdot (-\sin x) - 1$ $= \sin^2 x - 1$ $= -\cos^2 x$	<p>✓ $-\tan x$</p> <p>✓ $-\sin x$ ✓ $\frac{-\sin x}{\cos x}$</p> <p>✓ $\sin^2 x - 1$</p> <p>✓ answer</p> <p>(5)</p>
5.2.1	$\cos 215^\circ$ $= -\cos 35^\circ$ $= -m$	<p>✓ reduction</p> <p>✓ answer</p> <p>(2)</p>
5.2.2	$\sin 20^\circ$ $= \cos 70^\circ$ $= \cos 2(35^\circ)$ $= 2\cos^2 35^\circ - 1$ $= 2m^2 - 1$ <p>OR</p> $= \sin(55^\circ - 35^\circ)$ $= \sin 55^\circ \cos 35^\circ - \cos 55^\circ \sin 35^\circ$ $= m \cdot m - \sqrt{1-m^2} \cdot \sqrt{1-m^2}$ $= m^2 - (1-m^2)$ $= 2m^2 - 1$	<p>✓ co-function</p> <p>✓ double angle expansion</p> <p>✓ answer in terms of m</p> <p>(3)</p> <p>✓ compound angle expansion</p> <p>✓ $\cos 55^\circ = \sqrt{1-m^2}$ or $\sin 35^\circ = \sqrt{1-m^2}$</p> <p>✓ answer in terms of m</p> <p>(3)</p>
5.3	$\cos 4x \cdot \cos x + \sin 4x \cdot \sin x = -0,7$ $\cos(4x - x) = -0,7$ $\text{ref } \angle = 45,57\dots^\circ$ $3x = 180^\circ - 45,57\dots^\circ + k \cdot 360^\circ \text{ or } 3x = 180^\circ + 45,57\dots^\circ + k \cdot 360^\circ$ $3x = 134,43^\circ + k \cdot 360^\circ \quad \text{or} \quad 3x = 225,57^\circ + k \cdot 360^\circ$ $x = 44,81^\circ + k \cdot 120^\circ; k \in \mathbb{Z} \quad x = 75,19^\circ + k \cdot 120^\circ; k \in \mathbb{Z}$	<p>✓ compound angle</p> <p>✓ $3x = 134,43^\circ$ or $225,57^\circ$</p> <p>✓ $x = 44,81^\circ$ or $75,19^\circ$</p> <p>✓ $+ k \cdot 120^\circ; k \in \mathbb{Z}$</p> <p>(4)</p>

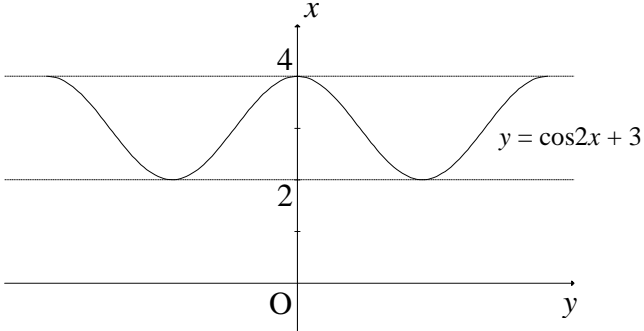
5.4	$\text{RHS} = \cos^2 x - \sin^2 x$ $\text{LHS} = \frac{\sin 4x \cdot \cos 2x - 2 \cos 4x \cdot \sin x \cdot \cos x}{\tan 2x}$ $= \frac{\sin 4x \cdot \cos 2x - \cos 4x \cdot \sin 2x}{\frac{\sin 2x}{\cos 2x}}$ $= \sin(4x - 2x) \left(\frac{\cos 2x}{\sin 2x} \right)$ $= \cos 2x$ $= \cos^2 x - \sin^2 x$ $\text{LHS} = \text{RHS}$	$\checkmark \sin 2x$ $\checkmark \frac{\sin 2x}{\cos 2x}$ $\checkmark \sin(4x - 2x)$ $\checkmark \cos 2x$
		(4)
		[18]

QUESTION/VRAAG 6

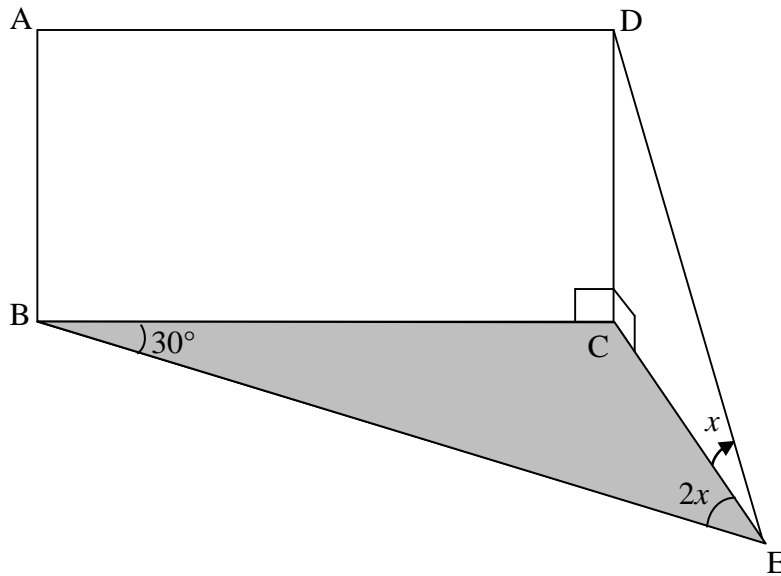
<p>6.1</p>	$1 - 2\sin^2 x = -\sin x$ $2\sin^2 x - \sin x - 1 = 0$ $(2\sin x + 1)(\sin x - 1) = 0$ $\sin x = -\frac{1}{2} \qquad \text{or} \qquad \sin x = 1$ $\text{ref } \angle = 30^\circ \qquad \text{ref } \angle = 90^\circ$ $x = 210^\circ + k.360^\circ \qquad x = 90^\circ + k.360^\circ$ $\text{or } x = 330^\circ + k.360^\circ$ $x = -150^\circ \text{ or } x = -30^\circ \text{ or } x = 90^\circ$ <p>OR</p> $\cos 2x = -\sin x$ $\cos 2x = -\cos(90^\circ - x)$ $2x = 180^\circ - (90^\circ - x) + k.360^\circ \text{ or } 2x = 180^\circ + (90^\circ - x) + k.360^\circ$ $2x = 90^\circ + x + k.360^\circ \text{ or } 2x = 270^\circ - x + k.360^\circ$ $x = 90^\circ + k.360^\circ \qquad x = 90^\circ + k.120^\circ$ $x = -150^\circ \text{ or } x = -30^\circ \text{ or } x = 90^\circ$ <p>OR</p> $\cos 2x = -\sin x$ $\cos 2x = \cos(90^\circ + x)$ $2x = 90^\circ + x + k.360^\circ \text{ or } 2x = 360^\circ - (90^\circ + x) + k.360^\circ$ $x = 90^\circ + k.360^\circ \text{ or } 3x = 270^\circ + k.360^\circ$ $\qquad \qquad \qquad x = 90^\circ + k.120^\circ$ $x = -150^\circ \text{ or } x = -30^\circ \text{ or } x = 90^\circ$ <p>OR</p> $\cos 2x = -\sin x$ $\sin(90^\circ - 2x) = -\sin x$ $90^\circ - 2x = 180^\circ + x + k.360^\circ \text{ or } 90^\circ - 2x = 360^\circ - x + k.360^\circ$ $x = -30^\circ + k.120^\circ \qquad x = -270^\circ + k.360^\circ$ $x = -150^\circ \text{ or } x = -30^\circ \text{ or } x = 90^\circ$	<ul style="list-style-type: none"> ✓ identity ✓ factors ✓ $\sin x = -\frac{1}{2}$ ✓ $\sin x = 1$ ✓ -150° and -30° ✓ 90° (A) (6) ✓ co-functions ✓ $2x$ in quadrant 2 ✓ $2x$ in quadrant 3 ✓ both general solutions ✓ -150° and -30° ✓ 90° (A) (6) ✓ co-functions ✓ $2x$ in quadrant 1 ✓ $2x$ in quadrant 4 ✓ both general solutions ✓ -150° and -30° ✓ 90° (A) (6) ✓ co-functions ✓ $90^\circ - 2x$ in quadrant 3 ✓ $90^\circ - 2x$ in quadrant 4 ✓ both general solutions ✓ -150° and -30° ✓ 90° (A) (6)
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6.2



<p>6.2.1</p>	<p>A(-150°; 0,5) B(-30°; 0,5) AB = -30° - (-150°) AB = 120°</p> <div style="border: 1px solid black; padding: 2px; display: inline-block;">Answer only: Full marks</div>	<p>✓ AB = -30° - (-150°) ✓ answer</p> <p style="text-align: right;">(2)</p>
<p>6.2.2</p>	<p>$x \in (0^\circ; 90^\circ)$ or $x \in (90^\circ; 180^\circ)$</p> <p>OR</p> <p>$0^\circ < x < 90^\circ$ or $90^\circ < x < 180^\circ$</p>	<p>✓ $x \in (0^\circ; 90^\circ)$ ✓ $x \in (90^\circ; 180^\circ)$</p> <p style="text-align: right;">(2)</p> <p>✓ $0^\circ < x < 90^\circ$ ✓ $90^\circ < x < 180^\circ$</p> <p style="text-align: right;">(2)</p>
<p>6.2.3</p>	<p>$\cos 2x = k - 3$ $k - 3 < -1$ or $k - 3 > 1$ $k < 2$ or $k > 4$</p> <p>OR</p> <div style="border: 1px solid black; padding: 2px; display: inline-block;">Answer only: Full marks</div>  <p>$k < 2$ or $k > 4$</p> <div style="border: 1px solid black; padding: 2px; display: inline-block;">Answer only: Full marks</div>	<p>✓ $k - 3 < -1$ or $k - 3 > 1$ ✓ $k < 2$ ✓ $k > 4$</p> <p style="text-align: right;">(3)</p> <p>✓ graph of $y = \cos 2x + 3$</p> <p>✓ $k < 2$ ✓ $k > 4$</p> <p style="text-align: right;">(3)</p>
<p>[13]</p>		

QUESTION/VRAAG 7

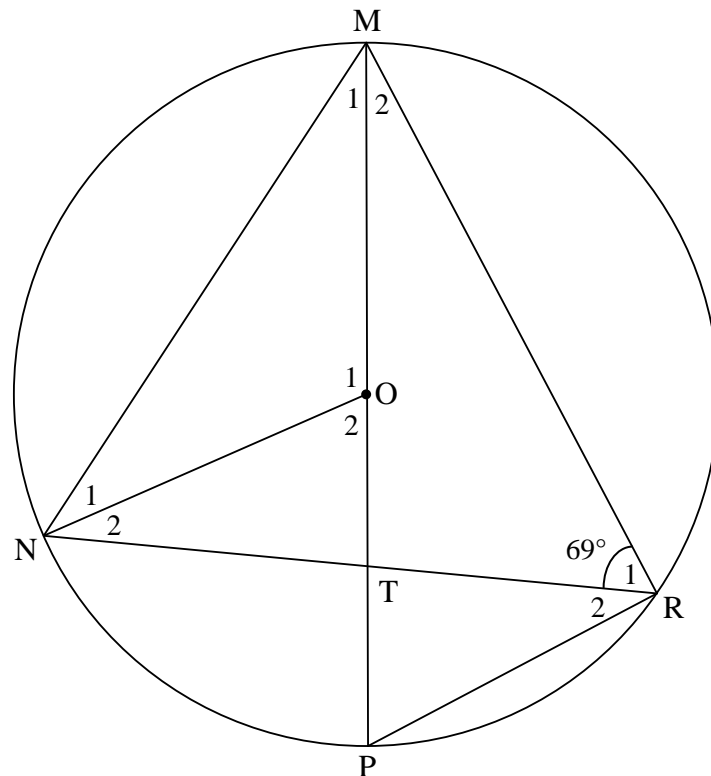


7.1	<p>In $\triangle BCE$:</p> $\frac{CE}{\sin \hat{B}} = \frac{BC}{\sin \hat{B}EC}$ $\frac{CE}{\sin 30^\circ} = \frac{BC}{\sin 2x}$ $CE = \frac{BC \sin 30^\circ}{\sin 2x}$ <p>In $\triangle CDE$:</p> $\frac{DC}{CE} = \tan \hat{D}EC$ $DC = \frac{BC \cdot \sin 30^\circ}{\sin 2x} (\tan x)$ $DC = \frac{BC}{4 \sin x \cos x} \left(\frac{\sin x}{\cos x} \right)$ $DC = \frac{BC}{4 \cos^2 x}$	<p>✓ correct use of sine rule</p> <p>✓ $CE = \frac{BC \sin 30^\circ}{\sin 2x}$</p> <p>✓ correct trig ratio</p> <p>✓ Subst CE</p> <p>✓ $2 \sin x \cos x \quad \checkmark \frac{\sin x}{\cos x}$</p> <p style="text-align: right;">(6)</p>
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7.2	$DC = \frac{BC}{4 \cos^2 30^\circ}$ $= \frac{BC}{4 \left(\frac{\sqrt{3}}{2} \right)^2}$ $= \frac{BC}{3}$ $\therefore BC = 3DC$ <p>But $AB = DC$ [opp sides of rectangle/<i>teenoorst. sye v reghoek</i>]</p> $\therefore BC = 3AB$ <p>Area of rectangle $= (AB)(BC)$ $= (AB)(3AB)$ $= 3AB^2$</p>	$\checkmark DC = \frac{BC}{3}$ $\checkmark BC = 3AB$ $\checkmark \text{ substitution into area formula}$ <p style="text-align: right;">(3)</p>
[9]		

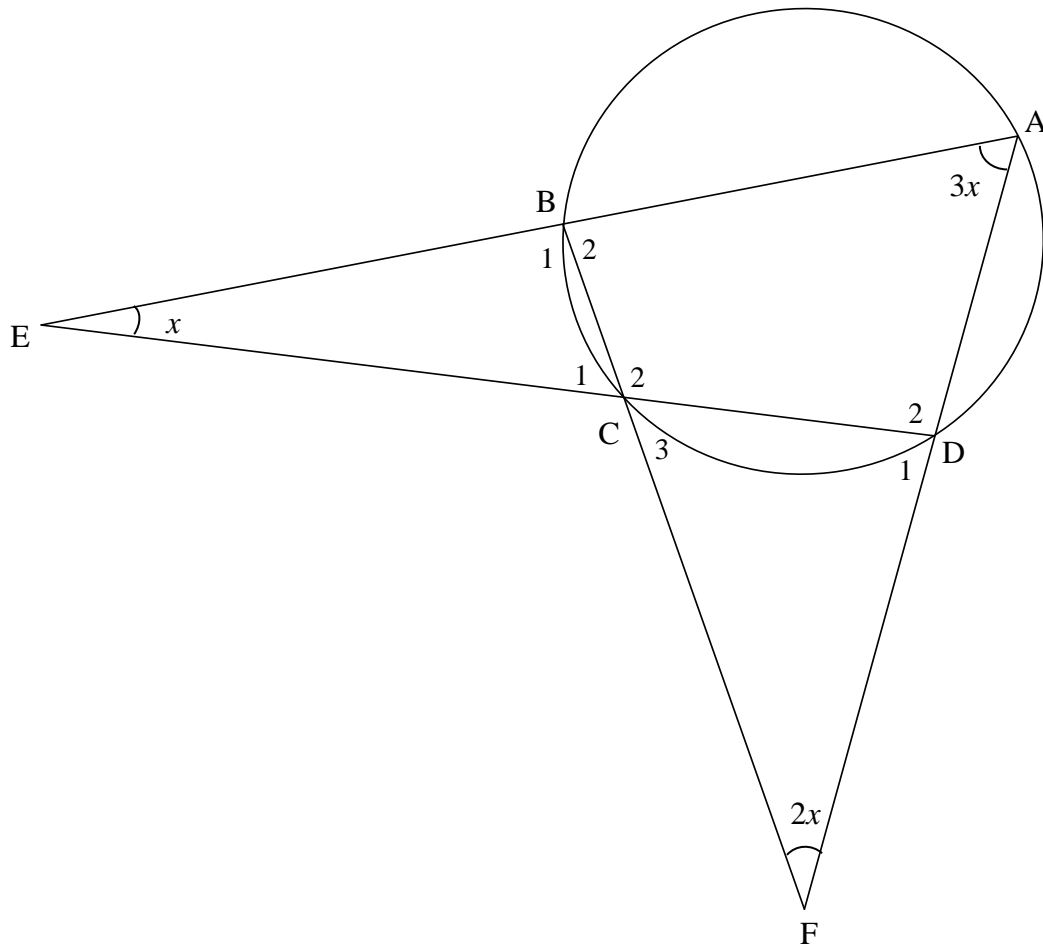
QUESTION/VRAAG 8

8.1



8.1.1	$\hat{M}\hat{R}P = 90^\circ$ $\hat{R}_2 = 21^\circ$	[\angle in semi circle/ \angle in halwe sirkel]	\checkmark R \checkmark S	(2)
8.1.2	$\hat{O}_1 = 138^\circ$	[\angle at centre = $2 \times \angle$ at circumference/ midpts. $\angle = 2 \times$ omtreks \angle]	\checkmark S \checkmark R	(2)
8.1.3	$\hat{M}_1 = 21^\circ$ OR $\hat{M}_1 + N_1 = 180^\circ - 138^\circ$ $\therefore \hat{M}_1 = 21^\circ$	[\angle s in the same segment/ \angle e in dieselfde sirkel segment] [sum of \angle s in Δ / \angle e v Δ] [\angle s opp equal sides/ \angle e teenoor gelyke sye]	\checkmark S \checkmark R \checkmark S \checkmark R	(2)
8.1.4	$\hat{O}_2 = 42^\circ$ $\hat{P} = 42^\circ$ $\hat{M}_2 = 48^\circ$ OR $\hat{N}_2 = \hat{R}_2 = 21^\circ$ $\hat{N}_1 = \hat{M}_1 = 21^\circ$ $\hat{M}_2 = 48^\circ$	[\angle s on a str line/ \angle e op 'n reguitlyn] [alt \angle s; NO \parallel PR/ <i>Verw. \anglee, NO \parallel PR</i>] [sum of \angle s in Δ / \angle e v Δ] [alt \angle s; NO \parallel PR/ <i>Verw. \anglee, NO \parallel PR</i>] [\angle s opposite equal sides/ \angle e teenoor gelyke sye] [sum of \angle s of Δ NMR// \angle e v Δ NMR]	\checkmark S \checkmark S \checkmark R \checkmark S \checkmark S \checkmark R \checkmark S \checkmark S	(4)

8.2

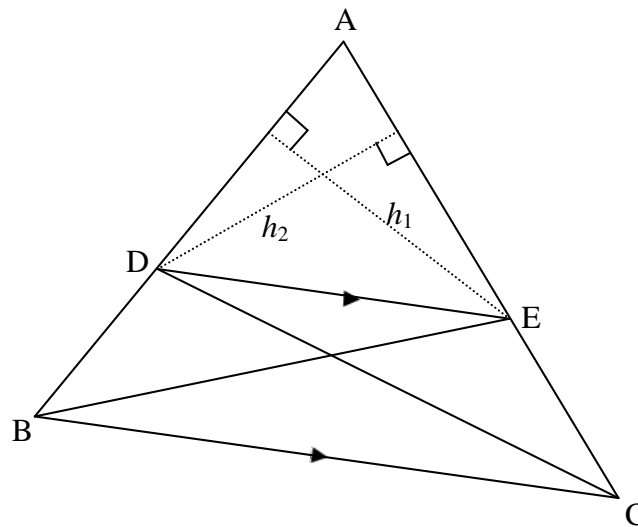


<p>8.2</p>	$\hat{D}_1 = 4x$ $\hat{D}_2 = 180^\circ - 4x$ $\hat{B}_1 = 5x$ $\hat{B}_1 = \hat{D}_2$ $180^\circ - 4x = 5x$ $9x = 180^\circ$ $x = 20^\circ$ <p>OR</p> $\hat{C}_1 = 3x$ $\hat{B}_2 = 4x$ $\hat{C}_1 = \hat{C}_3 = 3x$ $\hat{D}_2 = 5x$ $4x + 5x = 180^\circ$ $x = 20^\circ$	<p>[ext \angle of Δ/buite \angle v Δ] [\angles on a str line/\anglee op 'n reguitlyn] [ext \angle of Δ/buite \angle v Δ] [ext \angle of cyclic quad/buite \angle v kvh] [ext \angle of cyclic quad/buite \angle v kvh] [ext \angle of Δ/buite \angle v Δ] [vert opp \angles] [ext \angle of Δ/buite \angle v Δ] [opp \angle of cyclic quad/teenoorst. \anglee v kvh]</p>	<p>✓ S/R ✓ S ✓ S ✓ S ✓ R ✓ answer (6) ✓ S ✓ R ✓ S ✓ S ✓ S/R ✓ answer (6)</p>
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	<p>OR</p> <p>$\hat{C}_3 = 3x$ [ext \angle of cyclic quad/buite \angle v kvh]</p> <p>$\hat{D}_1 = 4x$ [ext \angle of Δ/buite \angle v Δ]</p> <p>$2x + 3x + 4x = 180^\circ$ [sum of \angles in Δ/\anglee v Δ]</p> <p>$9x = 180^\circ$</p> <p>$x = 20^\circ$</p>	<p>✓ S ✓R</p> <p>✓ S</p> <p>✓ S ✓R</p> <p>✓ answer</p> <p>(6)</p>
[16]		

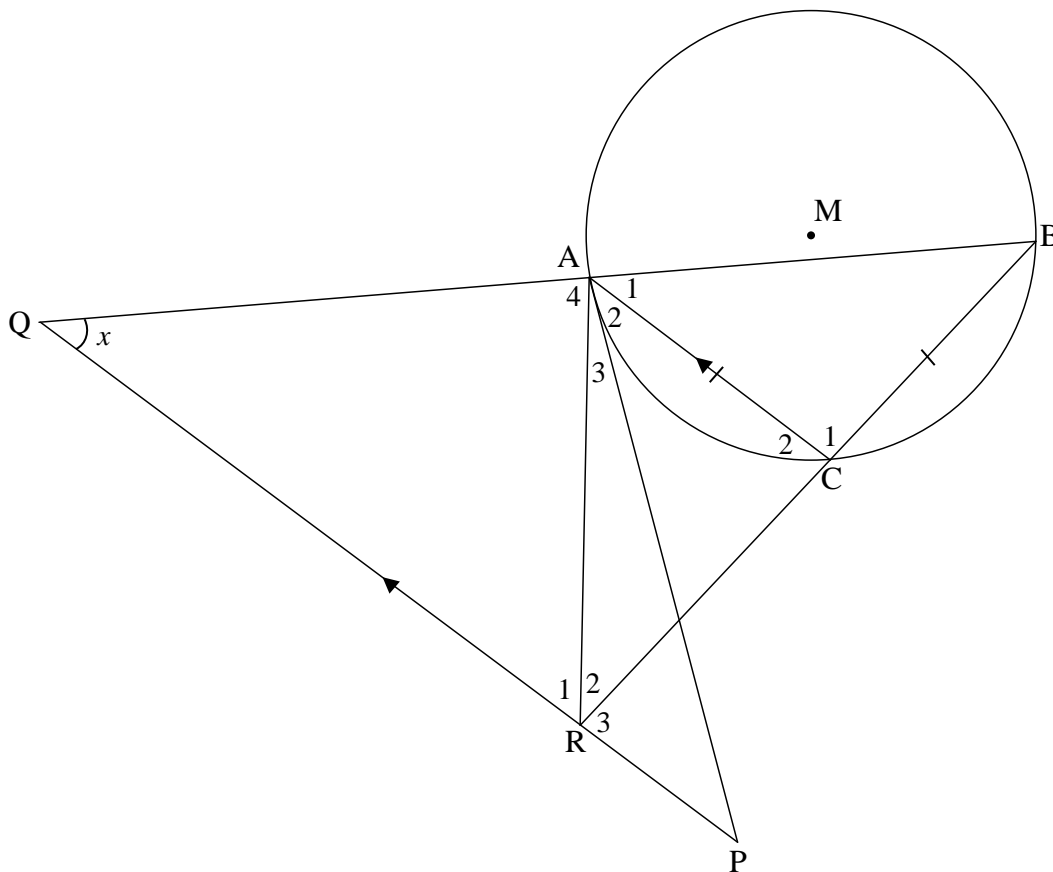
QUESTION/VRAAG 9

9.1



<p>9.1</p>	<p>Constr: Join BE and CD and draw h_1 from E \perp AD and h_2 from D \perp AE</p> <p><i>Konstr: Verbind BE en CD en trek h_1 vanaf E \perp AD en h_2 vanaf D \perp AE</i></p> <p>Proof/Bewys:</p> $\frac{\text{area } \triangle ADE}{\text{area } \triangle BDE} = \frac{\frac{1}{2}AD \times h_1}{\frac{1}{2}BD \times h_1} = \frac{AD}{BD}$ $\frac{\text{area } \triangle ADE}{\text{area } \triangle DEC} = \frac{\frac{1}{2}AE \times h_2}{\frac{1}{2}EC \times h_2} = \frac{AE}{EC}$ <p>area $\triangle ADE$ = area $\triangle ADE$ [common/gemeenskaplik]</p> <p>But area $\triangle BDE$ = area $\triangle DEC$ [same base & height ; DE \parallel BC/ <i>dies basis & hoogte ; DE \parallel BC]</i></p> $\therefore \frac{\text{area } \triangle ADE}{\text{area } \triangle BDE} = \frac{\text{area } \triangle ADE}{\text{area } \triangle DEC}$ $\therefore \frac{AD}{BD} = \frac{AE}{EC}$	<p>✓ constr/konstr</p> $\frac{\text{area } \triangle ADE}{\text{area } \triangle BDE}$ $\frac{\frac{1}{2}AD \times h_1}{\frac{1}{2}BD \times h_1} \text{ or R}$ $\frac{\text{area } \triangle ADE}{\text{area } \triangle DEC} = \frac{AE}{EC}$ <p>✓ S ✓R</p> <p>(6)</p>
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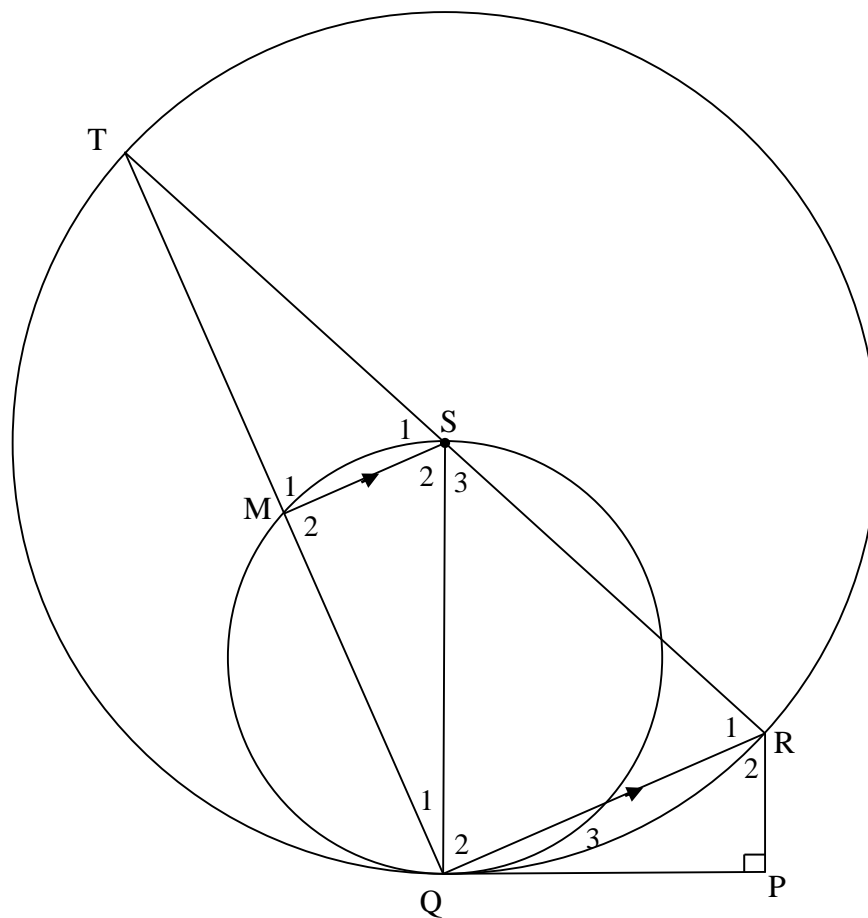
9.2



<p>9.2.1</p>	<p>$\hat{A}_1 = x$ [corresp \angles; $PQ \parallel CA$/ooreenkomstige \anglee, $PQ \parallel CA$] $\hat{B} = x$ [\angles opp equal sides/\anglee teenoor gelyke sye] $\hat{A}_2 = x$ [tan-chord theorem/\angle tussen raaklyn en koord] $\hat{P} = x$ [alt \angles; $PQ \parallel CA$/verw. \anglee, $PQ \parallel CA$]</p>	<p>✓ S ✓ R ✓ S/R ✓ S ✓ R ✓ S/R</p>
<p>9.2.2</p>	<p>$\hat{B} = \hat{P}$ [proved in 9.2.1/bewys in 9.2.1] \therefore A, B, P and R are concyclic \therefore ABPR is a cyclic quadrilateral [conv \angles in the same segment/ koord onderspan gelyke omtreks \anglee]</p>	<p>✓ S ✓ R</p>
<p>9.2.3</p>	<p>$\frac{BA}{BQ} = \frac{BC}{BR}$ [prop th; $AC \parallel QP$] OR [line \parallel one side Δ/lyn \parallel een syn v Δ] But $QR = BR$ [sides opp = \angles/sye teenoor = \anglee] $\therefore \frac{BA}{BQ} = \frac{BC}{QR}$</p>	<p>✓ S ✓ R ✓ S</p>

	<p>OR</p> <p>In ΔABC and ΔBQR:</p> <p>$\hat{A}_1 = \hat{B} = x$ [proved in 9.2.1]</p> <p>$\hat{B} = \hat{Q} = x$ [proved in 9.2.1]</p> <p>$\hat{C}_1 = \hat{B}RQ = 180^\circ - 2x$ [sum of \angles of Δ]</p> <p>$\therefore \Delta ABC \parallel \Delta BQR$</p> <p>$\therefore \frac{BA}{BQ} = \frac{BC}{QR}$</p>	<p>✓ S</p> <p>✓ S</p> <p>✓ S</p> <p>(3)</p>
	<p>OR</p> <p>In ΔABC and ΔBQR:</p> <p>$\hat{A}_1 = \hat{B} = x$ [proved in 9.2.1]</p> <p>$\hat{B} = \hat{Q} = x$ [proved in 9.2.1]</p> <p>$\hat{C}_1 = \hat{B}RQ = 180^\circ - 2x$ [sum of \angles of Δ]</p> <p>$\therefore \Delta ABC \parallel \Delta BQR$ [$\angle\angle\angle$]</p> <p>$\therefore \frac{BA}{BQ} = \frac{BC}{QR}$</p>	<p>✓ S</p> <p>✓ S</p> <p>✓ R</p> <p>(3)</p>
	<p>OR</p> <p>In ΔABC and ΔQBR:</p> <p>\hat{B} is common</p> <p>$\hat{A}_1 = \hat{Q} = x$ [corres \angles; $PQ \parallel CA$]</p> <p>$\hat{C}_1 = \hat{B}RQ = 180^\circ - 2x$ [sum of \angles of Δ]</p> <p>$\therefore \Delta ABC \parallel \Delta QBR$ [$\angle\angle\angle$]</p> <p>But $QR = BR$ [sides opp = \angles/sye teenoor = \anglee]</p> <p>$\therefore \frac{BA}{BQ} = \frac{BC}{QR}$</p>	<p>✓ S</p> <p>✓ S</p> <p>✓ S</p> <p>(3)</p>
<p>[17]</p>		

QUESTION/VRAAG 10



<p>10.1.1</p>	<p>$\hat{Q}_1 + \hat{Q}_2 = 90^\circ$ $\therefore \hat{M}_2 = 90^\circ$ $\therefore SQ$ is a diameter</p> <p>OR $MS \parallel QR$ $\frac{TS}{SR} = \frac{TM}{MQ} = \frac{1}{1}$ $\therefore TM = MQ$ $\therefore \hat{M}_2 = 90^\circ$ $\therefore SQ$ is a diameter</p> <p>OR $SQ \perp QP$ $\therefore SQ$ is a diameter</p>	<p>[\angle in semi circle/\angle in halwe sirkel] [co-interior \angle, $MS \parallel QR$/ko-binne \anglee, $MS \parallel QR$] [converse: \angle in semi circle/ <i>Omgekeerde: \angle in halwe sirkel]</i></p> <p>[prop theorem; $SM \parallel QR$] OR [line \parallel one side of Δ]/lyn \parallel een sy vΔ</p> <p>[Line from centre bisects chord/<i>midpt. sirkel; midpt koord</i>] [converse: \angle in semi circle/ <i>Omgekeerde: \angle in halwe sirkel]</i></p> <p>[tan \perp rad/<i>raaklyn \perp radius</i>] [converse: tan \perp rad/<i>Omgekeerde: raaklyn \perp radius</i>]</p>	<p>✓ S/R ✓ S/R ✓ R (3)</p> <p>✓ S/R ✓ R (3)</p> <p>✓ S ✓ R ✓ R (3)</p>
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<p>10.1.2</p>	<p>In $\triangle RTQ$ and $\triangle RQP$ $\hat{T} = \hat{Q}_3$ [tan-chord theorem/<i>∠ tussen raaklyn en koord</i>] $\hat{Q}_1 + \hat{Q}_2 = 90^\circ$ [co-interior \angles, $MS \parallel QR$/<i>ko-binne ∠e, MS \parallel QR</i>] or [\angle in semi circle/<i>∠ in halwe sirkel</i>] $\therefore \hat{Q}_1 + \hat{Q}_2 = \hat{P} = 90^\circ$ $\hat{R}_1 = \hat{R}_2$ [\angles of Δ/<i>∠e van Δ</i>] $\triangle RTQ \parallel \triangle RQP$ $\frac{RT}{RQ} = \frac{RQ}{RP}$ $RT = \frac{RQ^2}{RP}$ OR In $\triangle RTQ$ and $\triangle RQP$ $\hat{T} = \hat{Q}_3$ [tan-chord theorem <i>∠ tussen raaklyn en koord</i>] $\hat{Q}_1 + \hat{Q}_2 = 90^\circ$ [co-interior \angles, $MS \parallel QR$/<i>ko-binne ∠e, MS \parallel QR</i>] or [\angle in semi circle/<i>∠ in halwe sirkel</i>] $\therefore \hat{Q}_1 + \hat{Q}_2 = \hat{P} = 90^\circ$ $\triangle RTQ \parallel \triangle RQP$ [\angle, \angle, \angle] $\frac{RT}{RQ} = \frac{RQ}{RP}$ $RT = \frac{RQ^2}{RP}$</p>	<p>✓ S ✓ R ✓ S ✓ S ✓ S ✓ ratio (6) ✓ S ✓ R ✓ S ✓ S ✓ R ✓ ratio (6)</p>
<p>10.2</p>	<p>$QR = 28$ units [midpoint theorem/<i>midpt. stelling</i>] $RP^2 = 28^2 - (\sqrt{640})^2$ [Pythagoras/<i>Pythagoras</i>] $RP = 12$ units $RT = \frac{RQ^2}{RP}$ $RT = \frac{28^2}{12}$ $RT = \frac{196}{3}$ Radius = $\frac{98}{3}$ units</p>	<p>✓ S ✓ R ✓ S ✓ $RP = 12$ ✓ RT ✓ answer (6)</p>
		<p>[15]</p>

TOTAL/TOTAAL: 150